MATHEMATICS STANDARD ARTICULATED BY GRADE LEVEL

Strand 1: Number and Operations

| CONCEPT | 2008 PO | ITEM DESCRIPTION | 2003 PO | ITEM DESCRIPTION |
|--------------------|---------|--|---------|---|
| 1. Number Sense | 1 | Express whole numbers through six digits using models, pictures, symbols, spoken and | 1 | Read whole numbers in contextual situations (through six-digit numbers). |
| | | written words, and/or expanded notation. | 2 | Identify six-digit whole numbers in or out of order. |
| | | | 3 | Write whole numbers through six-digits in or out of order. |
| | | | 4 | State whole numbers, through six-digits, with correct place value, by using models, illustrations, symbols, or expanded notation (e.g., 53,941 = 50,000 + 3,000 + 900 + 40 +1). |
| | | | 5 | Construct models to represent place value concepts for the one's, ten's, and hundred's places. |
| | | | 6 | Apply expanded notation to model place value through 9,999 (e.g., 5,378 = 5,000 + 300 + 70 + 8). |
| | 2 | Compare and order three or more whole numbers through six digits by applying the | 8 | Compare two whole numbers, through six-digits. |
| | | concept of place value using symbols (<, >, =, ≠). | 9 | Order three or more whole numbers through six-digit numbers (least to greatest, or greatest to least). |

^{*} This performance objective is new to the 2008 Draft Mathematics Standard Articulated by Grade Level.

| | | Strand 1: Number and Op | erations | |
|--------------------|---------|--|----------|---|
| CONCEPT | 2008 PO | ITEM DESCRIPTION | 2003 PO | ITEM DESCRIPTION |
| 1. Number Sense | 3 | Identify the place value and actual value of digits for whole numbers up to six digits. | 4 | State whole numbers, through six-digits, with correct place value, by using models, illustrations, symbols, or expanded notation (e.g., 53,941 = 50,000 + 3,000 + 900 + 40 +1). |
| | 4 | Sort numbers into sets and justify the sort. | 7 | Sort whole numbers into sets containing only odd numbers or only even numbers. |
| | 5 | Count and represent money using coins and bills up to \$20.00. | 15 | Count amounts of money through \$20.00 using pictures or actual bills and coins |
| | 6 | Describe benchmark fractions as: • fair sharing parts of whole, | 10 | Make models that represent proper fractions (halves, thirds, fourths, eighths, and tenths). |
| | | parts of a set, and as locations on a number line. | 11 | Identify symbols, words, or models that represent proper fractions (halves, thirds, fourths, eighths and tenths). |
| | 7 | Express benchmark fractions using models, symbols, and written and spoken words in and out of context. | 10 | Make models that represent proper fractions (halves, thirds, fourths, eighths, and tenths). |
| | | | 11 | Identify symbols, words, or models that represent proper fractions (halves, thirds, fourths, eighths and tenths). |
| | | | 12 | Use proper fractions in contextual situations. |

^{*} This performance objective is new to the 2008 Draft Mathematics Standard Articulated by Grade Level.

| | | Strand 1: Number and O | perations | |
|--------------------|-----------------|--|-----------|--|
| CONCEPT | 2008 PO | ITEM DESCRIPTION | 2003 PO | ITEM DESCRIPTION |
| 1. Number Sense | 8 | Compare and order (<, >, =, ≠) benchmark fractions with like denominators. | 13 | Compare two proper fractions with like denominators. |
| | | | 14 | Order three or more proper fractions with like denominators (halves, thirds, fourths, eighths, and tenths). |
| | M03- S1C2-01 | Moved to Strand 1 Concept 2 | 16 | Use decimals through hundredths in contextual situations. |
| | | REMOVED | 17 | Compare two decimals, through hundredths, using models, illustrations, or symbols. |
| | | REMOVED | 18 | Order three or more decimals, through hundredths, using models, illustrations, or symbols. |
| | | REMOVED | 19 | Determine the equivalency among decimals, fractions, and percents (e.g., half-dollar = 50 ¢ = 50 % and $1/4$ = 0.25 = 25 %). |
| | | REMOVED | 20 | Identify whole-number factors and/or pairs of factors for a given whole number through 24. |
| | | REMOVED | 21 | Determine multiples of a given whole number with products through 24 (skip counting). |

^{*} This performance objective is new to the 2008 Draft Mathematics Standard Articulated by Grade Level.

| | | Strand 1: Number and Op | erations | |
|-------------------------|---------|--|----------|---|
| CONCEPT | 2008 PO | ITEM DESCRIPTION | 2003 PO | ITEM DESCRIPTION |
| 2. Numerical Operations | 1 | Add and subtract whole numbers to at least four digits, money to \$20.00, and fractions with | 2 | Add two three-digit whole numbers. |
| Орегалопа | | like denominators accurately, efficiently, and flexibly in contextual and non-contextual | 3 | Subtract two three-digit whole numbers. |
| | | situations. | 4 | Add a column of numbers. |
| | | | 5 | Select the grade-level appropriate operation to solve word problems. |
| | | | 6 | Solve word problems using grade-level appropriate operations and numbers. |
| | | | 17 | Apply addition and subtraction in contextual situations, through \$20.00. |
| | | | S1C1-16 | Use decimals through hundredths in contextual situations. |
| _ | 2 | Demonstrate the process of multiplication and division using multiple models. | 7 | Demonstrate the process of multiplication as repeatedly adding the same number, counting by multiples, combining equal sets, and making arrays. |
| | | | 8 | Demonstrate the process of division with one- digit divisors (separating elements of a set into smaller equal sets, sharing equally, or repeatedly subtracting the same number). |

^{*} This performance objective is new to the 2008 Draft Mathematics Standard Articulated by Grade Level.

| | | Strand 1: Number and Op | erations | |
|-------------------------|---------|--|----------|---|
| CONCEPT | 2008 PO | ITEM DESCRIPTION | 2003 PO | ITEM DESCRIPTION |
| 2. Numerical Operations | 3 | Use multiple strategies to develop fluency with multiplication and division through 10s in contextual and non-contextual situations. | 7 | Demonstrate the process of multiplication as repeatedly adding the same number, counting by multiples, combining equal sets, and making arrays. |
| | | | 8 | Demonstrate the process of division with one- digit divisors (separating elements of a set into smaller equal sets, sharing equally, or repeatedly subtracting the same number). |
| | | | 10 | State multiplication and division facts through 9s. |
| | 4 | Apply commutative and identity properties to multiplication and division. | 11 | Demonstrate the commutative and identity properties of multiplication. |
| | | | 12 | Identify multiplication and division as inverse operations. |
| | | | 13 | Apply grade-level appropriate properties to assist in computation. |
| | 5 | Apply the concept of multiplication and division as inverse operations to solve problems (fact families). | 9 | Demonstrate families of equations for multiplication and division through 9s. |
| | | REMOVED | 1 | Demonstrate the process of subtraction using manipulatives through three-digit whole numbers. |

^{*} This performance objective is new to the 2008 Draft Mathematics Standard Articulated by Grade Level.

| | | Strand 1: Number and Op | erations | |
|-------------------------|-----------------|---|----------|---|
| CONCEPT | 2008 PO | ITEM DESCRIPTION | 2003 PO | ITEM DESCRIPTION |
| 2. Numerical Operations | | REMOVED | 14 | Apply the symbols: \times , \div , $/$, $*$, $\%$, and the grouping symbols () and ",". |
| | | REMOVED | 15 | Use grade-level appropriate mathematical terminology. |
| | | REMOVED | 16 | Add or subtract fractions with like denominators (halves, thirds, fourths, eighths, and tenths) appropriate to grade level. |
| 3. Estimation | 1 | Use zero, half, and whole as benchmarks for estimating fractions.* | | |
| | 2 | Make estimates appropriate to a given situation with whole numbers by: | 1 | Solve grade-level appropriate problems using estimation. |
| | | knowing when to estimate, selecting an appropriate method of estimation, and determining the reasonableness of an estimate. | 5 | Evaluate the reasonableness of estimated measures. |
| | M03- S4C4-01 | Moved to Strand 4 Concept 4 | 2 | Estimate length and weight using U.S. customary units. |
| | M03- S4C4-01 | Moved to Strand 4 Concept 4 | 3 | Record estimated and actual linear measurements for real-life objects (e.g., length of fingernail; height of desk). |

^{*} This performance objective is new to the 2008 Draft Mathematics Standard Articulated by Grade Level.

| Strand 1: Number and Operations | | | | |
|---------------------------------|-----------------|-----------------------------|---------|---|
| CONCEPT | 2008 PO | ITEM DESCRIPTION | 2003 PO | ITEM DESCRIPTION |
| 3. Estimation | M03- S4C4-01 | Moved to Strand 4 Concept 4 | 4 | Compare estimations of appropriate measures to the actual measures. |

| CONCEPT | 2008 PO | ITEM DESCRIPTION | Discrete Ma | ITEM DESCRIPTION |
|----------------------------------|---------|--|-------------|---|
| | | | | |
| 1. Data Analysis (Statistics) | 1 | Collect, generate, organize, and display data in contextual situations using: | 2 | Construct a horizontal bar, vertical bar, pictograph, or tally chart with appropriate labels and title from organized data. |
| | | horizontal and vertical single bar graphs, line plots, and frequency tables. | | |
| | 2 | Analyze displays of data; formulate questions based on displays of data. | 3 | Interpret data found in line plots, pictographs, and single-bar graphs (horizontal and vertical). |
| | | | 4 | Answer questions based on data found in line plots, pictographs, and single-bar graphs (horizontal and vertical). |
| | | | 5 | Formulate questions based on graphs, charts, and tables to solve problems. |
| | | | 6 | Solve problems using graphs, charts and tables |

^{*} This performance objective is new to the 2008 Draft Mathematics Standard Articulated by Grade Level.

| | Strand 2: Data Analysis, Probability, and Discrete Mathematics | | | | | |
|----------------------------------|---|---|--|--|--|--|
| CONCEPT | 2008 PO | ITEM DESCRIPTION | 2003 PO | ITEM DESCRIPTION | | |
| 1. Data Analysis (Statistics) | | REMOVED | 1 | Formulate questions to collect data in contextual situations. | | |
| 2. Probability | 1 | Describe elements of theoretical probability: • name or draw all possible outcomes | 1 | Name the possible outcomes for a probability experiment. | | |
| | and • predict the outcome using "likely," "unlikely," "certain," or "impossible." | 2 | Make predictions about the probability of events being more likely, less likely, equally likely or unlikely. | | | |
| | 2 | Demonstrate elements of experimental probability: | 3 | Predict the outcome of a grade-level appropriate probability experiment. | | |
| | | predict specific outcomes based on manipulatives used with the experiment, | 4 | Record the data from performing a grade-level appropriate probability experiment. | | |
| | | perform experiment, record data, compare the outcome to the prediction, and | 5 | Compare the outcome of an experiment to predictions made prior to performing the experiment. | | |
| | | compare the results of multiple repetitions. | 6 | Compare the results of two repetitions of the same grade-level appropriate probability experiment. | | |

^{*} This performance objective is new to the 2008 Draft Mathematics Standard Articulated by Grade Level.

| | | Strand 2: Data Analysis, Probability, and | l Discrete Ma | thematics |
|---|---------|---|---------------|--|
| CONCEPT | 2008 PO | ITEM DESCRIPTION | 2003 PO | ITEM DESCRIPTION |
| 3. Discrete Mathematics – Systematic Listing and Counting | 1 | Solve a variety of problems based on the multiplication principle of counting.* | | |
| | 2 | Represent all possibilities for a variety of counting problems using arrays, charts, and systematic lists; draw conclusions from these representations.* | | |
| | | REMOVED | 1 | Make a diagram to represent the number of combinations available when 1 item is selected from each of 3 sets of 2 items (e.g., 2 different shirts, 2 different hats, 2 different belts). |
| 4. Discrete Mathematics – Vertex-Edge Graphs | 1 | Color the regions of maps and color the vertices of a vertex-edge graph using the fewest number of colors as an introduction to the general problem of avoiding conflicts.* | 1 | Color maps with the least number of colors so that no common edges share the same color (increased complexity throughout grade levels). |
| | 2 | Investigate simple properties of vertex-edge graphs: circuits in a graph, weights on edges, and shortest path between two vertices.* | | |

^{*} This performance objective is new to the 2008 Draft Mathematics Standard Articulated by Grade Level.

| | | Strand 3: Patterns, Algebra, ar | nd Functions | 5 |
|---------------------------------|---------|---|--------------|---|
| CONCEPT | 2008 PO | ITEM DESCRIPTION | 2003 PO | ITEM DESCRIPTION |
| 1. Patterns | 1 | Recognize, analyze, extend, and create or find missing terms in sequential numerical patterns and geometric patterns. | 2 | Extend a grade-level appropriate repetitive pattern (e.g., 5, 10, 15, 20, rule: add five or count by five's. |
| | | | 3 | Solve grade-level appropriate pattern problems. |
| | 2 | Explain the rule for a given numerical or symbolic pattern. | 1 | Communicate a grade-level appropriate iterative pattern, using symbols or numbers. |
| 2. Functions and Relationships | 1 | Describe, extend, or find the missing term(s) in a given function or rule with addition, subtraction, multiplication, or division.* | | |
| | 2 | Describe a rule that represents the relationship between two given sets of data which are on a table, model, input/output machine, etc. | 1 | Describe the rule used in a simple grade-level appropriate function (e.g., T-chart, input/output model, and frames and arrows). |
| 3. Algebraic Representations | 1 | Record equivalent forms of whole numbers up to six digits by constructing models.* | \ | |
| | 2 | Use symbols to represent variables in contextual situations. | 1 | Use variables in contextual situations. |

^{*} This performance objective is new to the 2008 Draft Mathematics Standard Articulated by Grade Level.

| Strand 3: Patterns, Algebra, and Functions | | | | | |
|--|---------|---|---------|---|--|
| CONCEPT | 2008 PO | ITEM DESCRIPTION | 2003 PO | ITEM DESCRIPTION | |
| 3. Algebraic Representations | 3 | Create and solve equations with one variable for addition and subtraction of whole numbers; create and solve equations with one variable for multiplication and division facts. | 2 | Solve equations with one variable using missing addends to sums of 18 (e.g., \square + 9 = 18, 9 + \square = 18); and using minuend through 18 (e.g., 18 - \square = 9, 18 - 9 = \square). | |
| 4. Analysis of Change | | REMOVED | 1 | Identify the change in a variable over time (e.g., an object gets taller, colder, heavier) | |
| | | REMOVED | 2 | Make simple predictions based on a variable (e.g., increases in allowance as you get older). | |

| Strand 4: Geometry and Measurement | | | | |
|------------------------------------|---------|---|---------|---|
| CONCEPT | 2008 PO | ITEM DESCRIPTION | 2003 PO | ITEM DESCRIPTION |
| 1. Geometric Properties | 1 | Identify and describe 3-dimensional figures including their relationship to real world objects: • sphere, • cube, • cone, • cylinder, and • rectangular prisms | 2 | Name concrete objects and pictures of 3-dimensional solids (cones, spheres, and cubes). |

^{*} This performance objective is new to the 2008 Draft Mathematics Standard Articulated by Grade Level.

| Strand 4: Geometry and Measurement | | | | | |
|------------------------------------|-----------------|--|--------|----|---|
| CONCEPT | 2008 PO | ITEM DESCRIPTION | 2003 F | 90 | ITEM DESCRIPTION |
| 1. Geometric Properties | 2 | Relate the shapes of the faces of 3-dimensional figures to 2-dimensional figures: • vertices/corners and • edges/sides. | 3 | | Describe relationships between 2-dimensional and 3-dimensional objects (squares/cubes, circles/spheres, triangles/cones). |
| | 3 | Describe patterns of geometric figures created by increasing the number of sides.* | | | |
| | 4 | Recognize similar figures. | 4 | | Recognize similar shapes. |
| | | REMOVED | 1 | | Build geometric figures with other common shapes (e.g., tangrams, pattern blocks, geoboards). |
| | M03-S4C2- 01 | Moved to Strand 4 Concept 3 | 5 | | Identify a line of symmetry in a 2-dimensional shape. |
| 2. Transformation of Shapes | 1 | Identify and justify all lines of symmetry, if any, in a 2-dimensional shape. | S4C2-(| 05 | Identify a line of symmetry in a 2-dimensional shape. |
| | 2 | Identify and demonstrate translations (slides), reflections (flips), and rotations (turns) using geometric figures. | 1 | | |
| 3. Coordinate Geometry | | Removed | 1 | | Identify points in the first quadrant of a grid using ordered pairs. |

^{*} This performance objective is new to the 2008 Draft Mathematics Standard Articulated by Grade Level.

Arizona Department of Education: Arizona Academic Content Standards

| Strand 4: Geometry and Measurement | | | | | |
|------------------------------------|---------|--|---------|---|--|
| CONCEPT | 2008 PO | ITEM DESCRIPTION | 2003 PO | ITEM DESCRIPTION | |
| 4. Measurement | 1 | Apply measurement skills to measure length, weight, and capacity using metric and U.S. customary units: • select the appropriate unit of measure (yd, pint, gallon, cm, m, mL, L, g, kg), | 1 | Select the appropriate measure of accuracy: • length – centimeters, meters, kilometers, • capacity/volume – liters, and • mass/weight – grams. | |
| | | select the appropriate tool, and estimate, measure, and compare estimate to actual measure. | 4 | Measure a given object using the appropriate unit of measure: | |
| | | | | length – centimeters, millimeters, meters kilometers, capacity/volume – liters, and mass/weight – grams. | |
| | 2 | across months using a calendar and by hours and half hours using a clock. | 3 | Determine the passage of time across months (units of days, weeks, months) using a calendar. | |
| | 3 | Read temperatures on a thermometer in metric and U.S. customary units. | 5 | Record temperatures to the nearest degree in degrees Fahrenheit and degrees Celsius as shown on a thermometer. | |

^{*} This performance objective is new to the 2008 Draft Mathematics Standard Articulated by Grade Level.

| Strand 4: Geometry and Measurement | | | | |
|------------------------------------|-----------------|---|---------|---|
| CONCEPT | 2008 PO | ITEM DESCRIPTION | 2003 PO | ITEM DESCRIPTION |
| 4. Measurement | 4 | Determine equivalent relationships for units of length, weight, and capacity: | 7 | Compare units of measure to determine more or less relationships for: • length – inches to feet; centimeters to meters, • time – minutes to hours; hours to days; days to weeks; months to years, and • money – pennies, nickels, dimes, quarters, and dollars. Determine relationships for: • volume – cups and gallons, • weight – ounces and pounds, and • money – extend to amounts greater than one dollar. |
| | 5 | Determine the area of a rectangular shape using an array model. | 10 | Represent area using a rectangular array. |
| | M02- S4C4-02 | Moved to Grade 2 | 2 | Tell time with one-minute precision (analog). |
| | | REMOVED | 8 | Compare the length of two objects using U.S. customary or metric units. |
| | | REMOVED | 9 | Determine the perimeter using a rectangular array. |

^{*} This performance objective is new to the 2008 Draft Mathematics Standard Articulated by Grade Level.

Arizona Department of Education: Arizona Academic Content Standards

| Strand 5: Structure and Logic | | | | |
|--|---------|--|---------|---|
| CONCEPT | 2008 PO | ITEM DESCRIPTION | 2003 PO | ITEM DESCRIPTION |
| 1. Algorithms and Algorithmic Thinking | 1 | Discriminate necessary information from unnecessary information in a given word problem. | 1 | Discriminate necessary information from unnecessary information in a given grade-level appropriate word problem. |
| 2. Logic, Reasoning, Arguments, and Mathematical Proof | 1 | Develop the problem-solving strategy of looking for a pattern.* | | |
| | 2 | Solve a non-routine problem by selecting and using a strategy.* | | |
| | 3 | Create written word problems using addition, subtraction, multiplication, or division.* | | |
| | | REMOVED | 1 | Draw conclusions based on existing information (e.g., All students in Ms. Dean's 1st grade class are less than 7 years old. Rafael is in Ms. Dean's class. Conclusion: Rafael is less than 7 years old.). |

^{*} This performance objective is new to the 2008 Draft Mathematics Standard Articulated by Grade Level.